

# Full Disk Encryption and Beyond

Monday, 15 July 2019



Louiza Khati

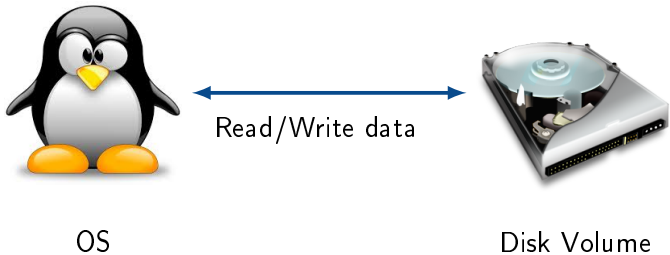
# Outline

- Part 1. From disk storage to security models
- Part 2. Key dependent-message security of Even-Mansour ciphers
- Part 3. Incremental MACs

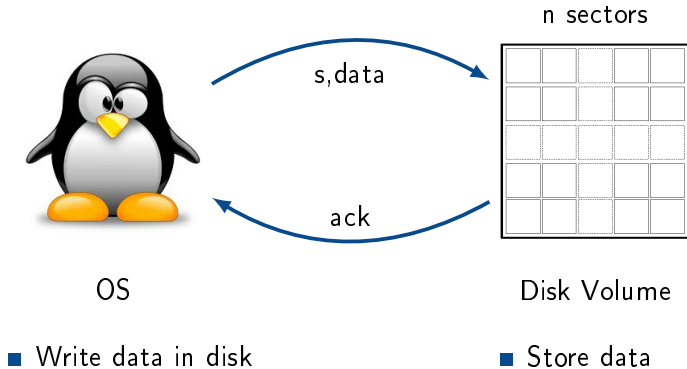
## Part 1.

# From Disk Storage to Security Models

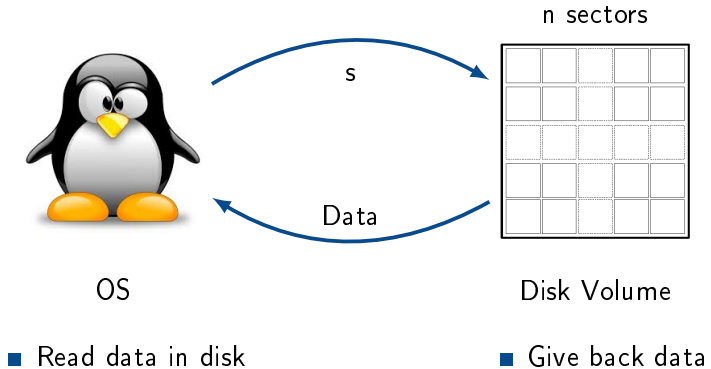
# Disk Storage



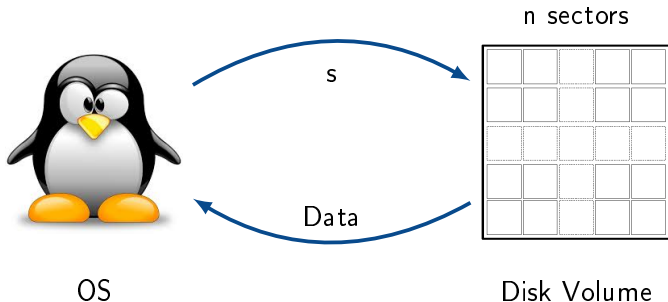
# Disk Storage: Write



# Disk Storage: Read



# Disk Storage: Performance



- Read/write speed is a priority (optimized)
- Competitive aspect for manufacturers

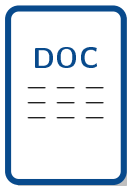
# Full Disk Encryption VS File Encryption

## ■ File encryption

- ▶ File content is encrypted
  - Title, file size encrypted?
- ▶ User action
  - Ask to encrypt a specific file
- ▶ Space for metadata
  - Better security using IV
  - Integrity

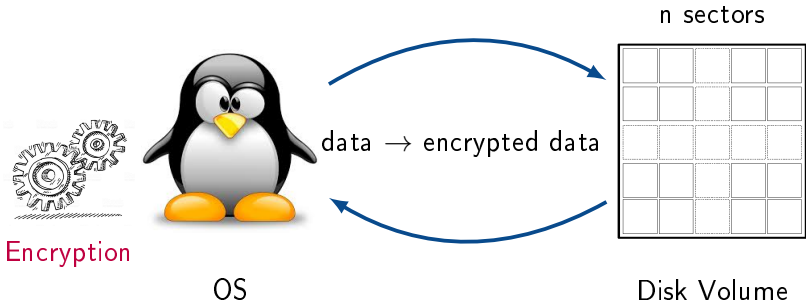
## ■ Full Disk Encryption

- ▶ All the data are encrypted
  - Sector-based encryption
- ▶ Transparent for the user
  - Automatic
- ▶ No space for metadata
  - No IVs
  - No Integrity



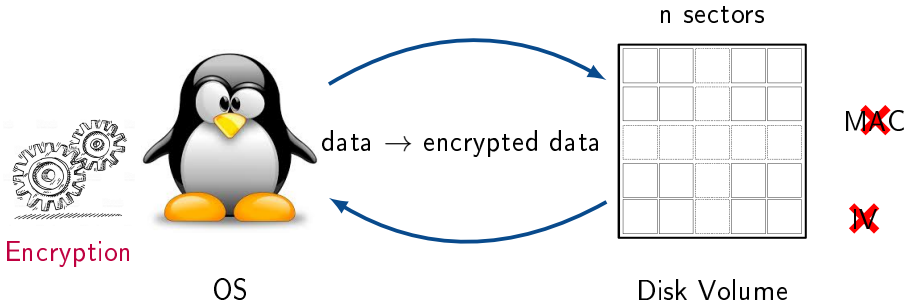


# Full Disk Encryption (FDE)



- Read and write: atomic operations
  - ▶ A sector is encrypted independently from the others

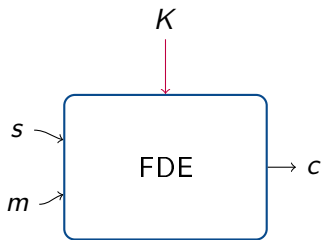
# Full Disk Encryption (FDE)



- Length preserving encryption (no metadata)
- Deterministic encryption

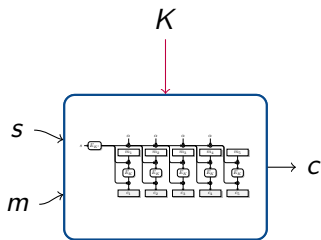


## FDE schemes



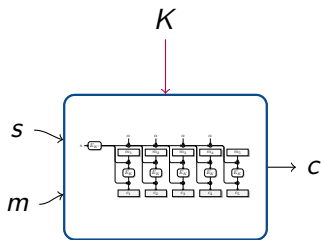
- Symmetric encryption (speed)
  - ▶ Blockciphers (AES)
  - ▶ Sector size  $>$  blockcipher input size

## FDE schemes



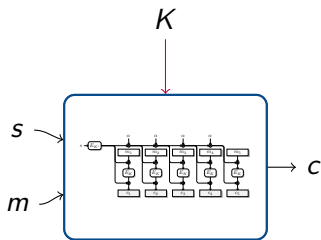
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  - ▶ Length preserving modes
  - ▶ Tweak  $s$  used to enhance security

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- Security proofs [K., Mouha, Vergnaud]
  - ▶ Reduction to blockcipher security
  - ▶ Different security notions

## FDE schemes



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- Security proofs [K., Mouha, Vergnaud]
  - ▶ Reduction to blockcipher security
  - ▶ Different security notions
- Examples (dm-crypt)
  - ▶ CBC-ESSIV
  - ▶ XTS (based on XEX)
  - ▶ Adiantum (new)

FDE tools: no control of what is stored!

## Full Disk Encryption and KDM security

- Atypical scenario can happen
  - ▶ The key can be stored in the disk
  - ▶ A (weird) function of the key can be stored



### Key-Dependent Message security Model

- Security analysis with an adversary that can ask to encrypt the key
- Key-Alternating Feistel ciphers [Farshim, K., Seurin, Vergnaud]
- Even-Mansour ciphers [Farshim, K., Vergnaud]

Part 2.

## Incremental MACs and "FDE"

Integrity → outside "FDE" Model!

How to get integrity with a minimal impact on performance?

- Authenticated Disk Encryption (ADE)
  - ▶ Ensures sector content integrity
  - ▶ MAC for each sector (a local tag/sector)
  - ▶ dm-integrity (Linux Kernel)



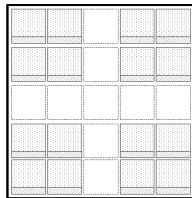
# Authenticated Disk Encryption

Authenticated  
Decryption



OS

n sectors



Disk Volume

■ Read a sector in disk

■ Give back sector content



# Authenticated Disk Encryption

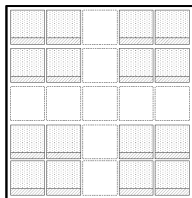
## Authenticated Encryption



OS

- Write a sector in disk

n sectors



Disk Volume

- Store sector content



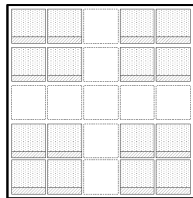
# Authenticated Disk Encryption



OS

Confidentiality  
+  
Integrity

n sectors



Disk Volume



## Incremental MACs and “FDE”

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Does not prevent replay-attacks!

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How to get integrity with a minimal impact on performance?

- Authenticated Disk Encryption (ADE)

- ▶ Ensures sector content integrity,
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- ▶ dm-integrity (Linux Kernel)

Does not prevent replay-attacks!

- Fully Authenticated Disk Encryption (FADE)

- ▶ Prevent replay-attacks
- ▶ Ensures local tags integrity
- ▶ MAC over all the local tags (global tag/disk)

# Fully Authenticated Disk Encryption

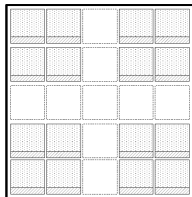


OS

Secure Memory



n sectors



Disk Volume

- Global tag = MAC over local tags
- Global tag in Secure memory (small)
- MAC is too expensive



# Fully Authenticated Disk Encryption

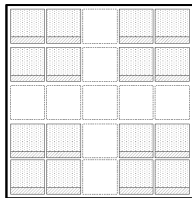


OS

Secure Memory



n sectors



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- Global tag = MAC over local tags
- Global tag in Secure memory (small)
- ~~MAC is too expensive~~ Incremental MACs



# Fully Authenticated Disk Encryption



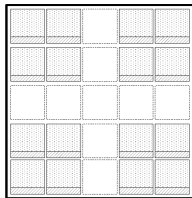
OS

Secure Memory



Confidentiality  
+  
Integrity  
+  
Anti-replay

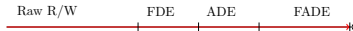
n sectors



Disk Volume

- Global tag = MAC over local tags
- Global tag in Secure memory (small)
- ~~MAC is too expensive~~ Incremental MACs

Part 3.





## Part 2.

# Key-Dependent Message (KDM) Security Even-Mansour Ciphers

## Security Analysis

- Robustness against an arbitrary adversary?



# Security Analysis

- Robustness against an arbitrary adversary?
- Robustness against specific attacks?
  - ▶ Specific to a blockcipher and not enough



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# Security Analysis

- Robustness against an **arbitrary adversary**?
- Robustness against **specific attacks**?
  - ▶ Specific to a blockcipher and not enough
- Robustness against **generic attacks**?
  - ▶ Feasible: Internal primitives idealized



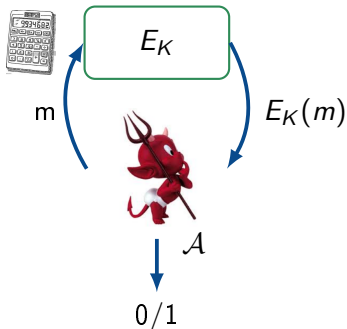
# Security Analysis

- Robustness against an arbitrary adversary?
- Robustness against specific attacks?
  - ▶ Specific to a blockcipher and not enough
- Robustness against generic attacks?
  - ▶ Feasible: Internal primitives idealized
- Security Proof
  - ▶ Modeled by a game: adversary/challenger
  - ▶ Adversary model (power)

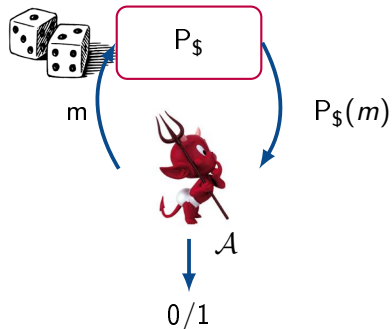


# Indistinguishability game

( $b=0$ ) Real world



( $b=1$ ) Random world

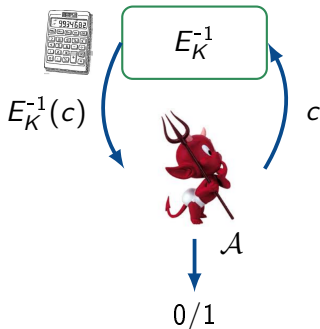


Chosen Plaintext Attack (CPA) adversary

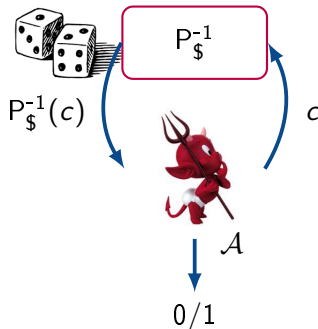
$$\mathbf{Adv} = | \Pr[\mathcal{A} \rightarrow 1 | \text{Real}] - \Pr[\mathcal{A} \rightarrow 1 | \text{Random}] |$$

# Indistinguishability game

(b=0) Real world



(b=1) Random world



Chosen Ciphertext Attack (CCA) adversary

$$\mathbf{Adv} = | \Pr[\mathcal{A} \rightarrow 1 | \text{Real}] - \Pr[\mathcal{A} \rightarrow 1 | \text{Random}] |$$



# KDM security: Indistinguishability game

(b=0) Real world



$K, E_K$

function  $\phi$

$E_K(\phi(K))$



$\mathcal{A}$

0/1

(b=1) Random world



$K, P_{\S}$

function  $\phi$

$P_{\S}(\phi(K))$



$\mathcal{A}$

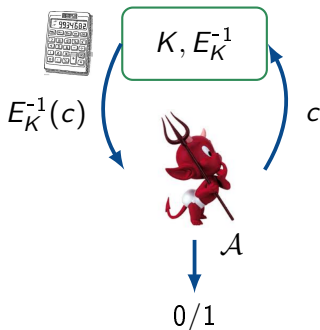
0/1

KDM-CPA adversary

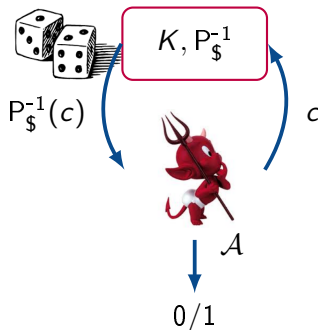
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## KDM security: Indistinguishability game

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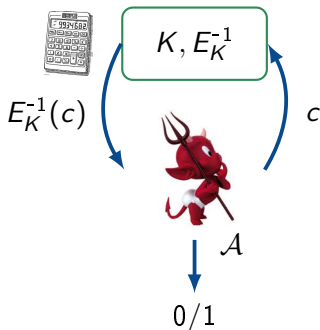


KDM-CCA adversary ("Standard" decryption)

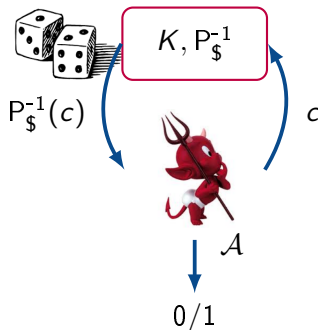
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# KDM security: Indistinguishability game

(b=0) Real world



(b=1) Random world



Forbidden queries: Repeat queries, Enc/Dec oracle's answers

## Key Dependent Message Security analysis

- Find the largest set  $\Phi$  of functions  $\phi$  such that Adv is small
  - ▶ Including constant functions
- What if  $\Phi$  is not restricted?

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Example: Projections

$$\phi_1(K) = (K \ \& \ 0\dots01)$$

If  $K = ?? \ 1$  then  $\phi_1(K) = 0\dots01$

If  $K = ?? \ 0$  then  $\phi_1(K) = 0\dots00$

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If  $K = ?? \ 1$  then  $\phi_1(K) = 0\dots 01$

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Using  $\phi_2$  and  $\phi_3$  such that:

$$\phi_2(K) = 0\dots 01$$

$$\phi_3(K) = 0\dots 00$$

## Key Dependent Message Security analysis

- Find the largest set  $\Phi$  of functions  $\phi$  such that Adv is small
  - ▶ Including constant functions
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Example: Projections

$$\phi_1(K) = (K \& 0\dots 01) \rightarrow c_1$$

$$\text{If } K = ??1 \text{ then } \phi_1(K) = 0\dots 01$$

$$\text{If } K = ??0 \text{ then } \phi_1(K) = 0\dots 00$$

Using  $\phi_2$  and  $\phi_3$  such that:

$$\phi_2(K) = 0\dots 01 \rightarrow c_2$$

$$\phi_3(K) = 0\dots 00 \rightarrow c_3$$

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Example: Projections

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$$\text{If } K = ???1 \text{ then } \phi_1(K) = 0\dots 01$$

$$\text{If } K = ???0 \text{ then } \phi_1(K) = 0\dots 00$$

If  $c_1 = c_2$  then

$K = ???1$  otherwise  $K = ???0$

Last bit recovered!!

Using  $\phi_2$  and  $\phi_3$  such that:

$$\phi_2(K) = 0\dots 01 \rightarrow c_2$$

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$$\phi_2(K) = 0\dots 01 \rightarrow c_2$$

$$\phi_3(K) = 0\dots 00 \rightarrow c_3$$

Key bits can be recovered one by one!

KDM set  $\Phi$  has to be restricted.

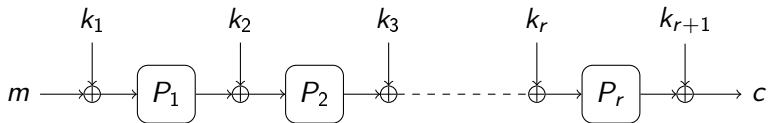
## KDM set restriction: Claw-freeness

Claw-freeness of a set  $\Phi$ :  $\forall \phi_1 \neq \phi_2, \Pr[\phi_1(K) = \phi_2(K)]$  is small.

KDM security:

- Ideal-Cipher KDM-secure under claw-free sets
  - ▶ [Farshim, K., Vergnaud].
- What about Even-Mansour ciphers?

## Even-Mansour ciphers



### ■ Configuration:

- ▶  $r$  rounds
- ▶  $r$  permutations ( $=$  or  $\neq$ )
- ▶ Key schedule:
  - $r + 1$  keys ( $=$  or  $\neq$ )
  - $r + 1$  keys derived from a master key

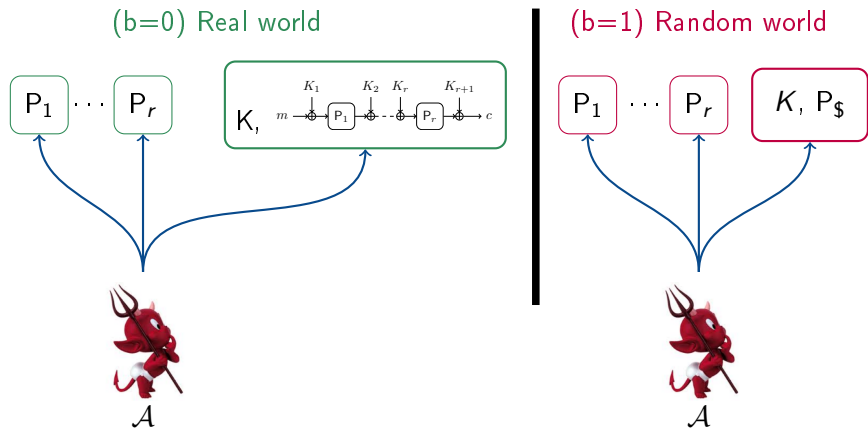
### ■ Previous security analysis

- ▶ Indistinguishability
- ▶ Related-key attack
- ▶ Indifferentiability

### ■ Examples:

- ▶ AES, SERPENT, PRESENT ...

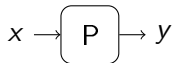
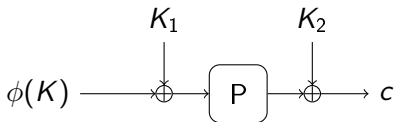
## Security analysis: Random permutation model



$P_i$  uniformly random permutations,  
KDM functions are oracle-independent ( $\phi^{P_i} \notin \text{KDM set } \Phi$ )

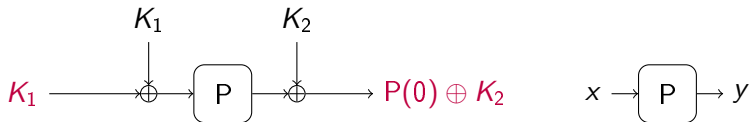
## KDM attack: 1-round Even-Mansour

A claw-free set  $\Phi$  not always enough...



## KDM attack: 1-round Even-Mansour

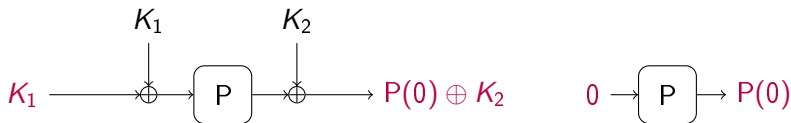
A claw-free set  $\Phi$  not always enough...



- Step 1. Challenge query  $\phi(K_1 || K_2) = K_1 \rightarrow c = P(0) \oplus K_2$

## KDM attack: 1-round Even-Mansour

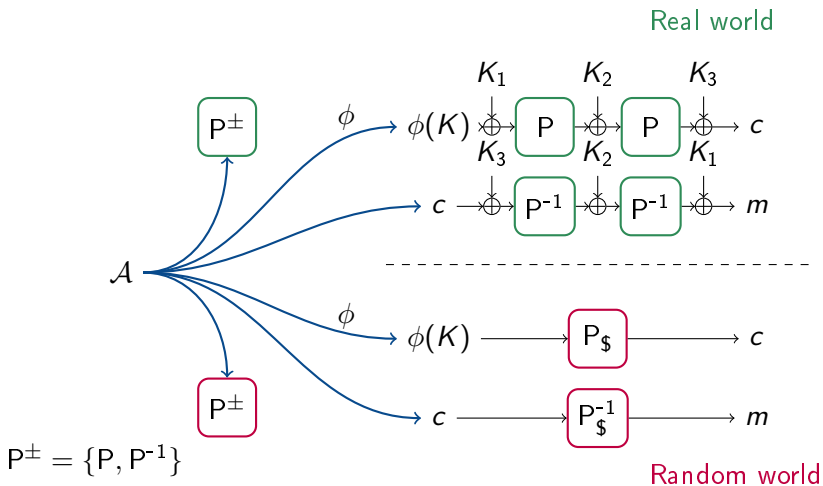
A claw-free set  $\Phi$  not always enough...



- Step 1. Challenge query  $\phi(K_1 || K_2) = K_1 \rightarrow c = P(0) \oplus K_2$
- Step 2. Direct query to  $P$   $x = 0 \rightarrow y = P(0)$
- Step 3.  $\mathcal{A}$  computes  $K_2 = c \oplus y$

Key extraction attack by a KDM adversary.

# KDM security analysis: 2-round Even-Mansour



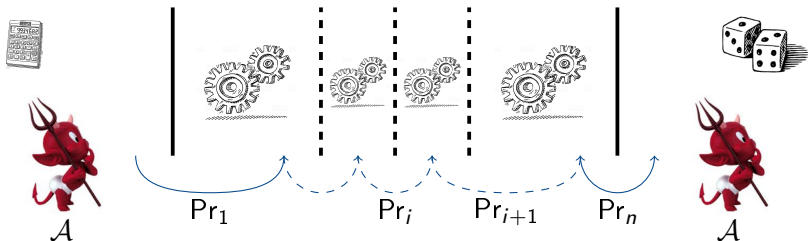
Restrictions on KDM set  $\Phi$  to have KDM security?



# KDM Security Analysis: Game playing

$(G_0)$  Real world

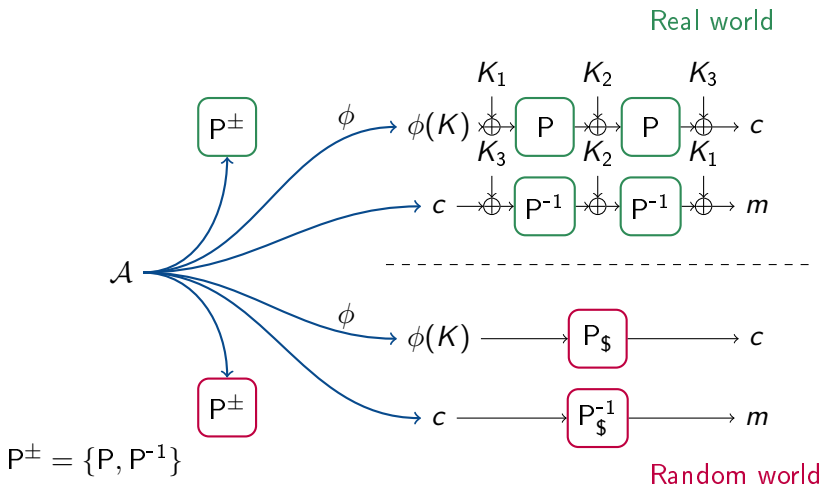
$(G_n)$  Random world



$$\Pr_i = \Pr[\mathcal{A} \text{ sets bad in } G_i]$$

- Adversary goal:
  - ▶ Trig bad events: distinguish real world from random world
- Fundamental lemma of game playing:  $\text{Adv} \leq \sum \Pr_i$

# KDM security analysis: Splitting and forgetting technique

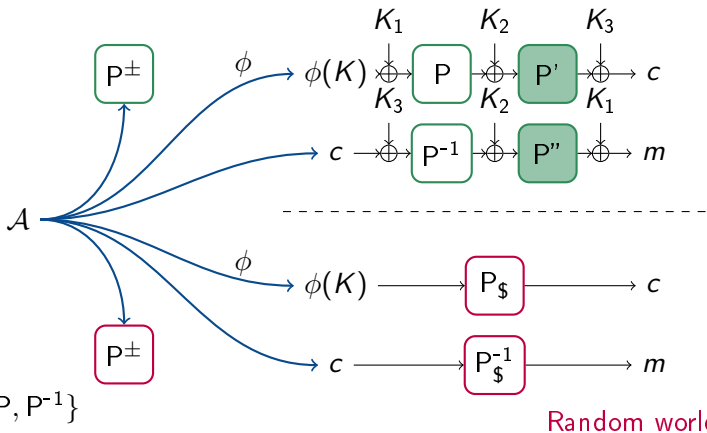


Application to 2r-EM same permutations, independent keys.

# KDM security analysis: Splitting and forgetting technique

“Oracle split”

Game 1

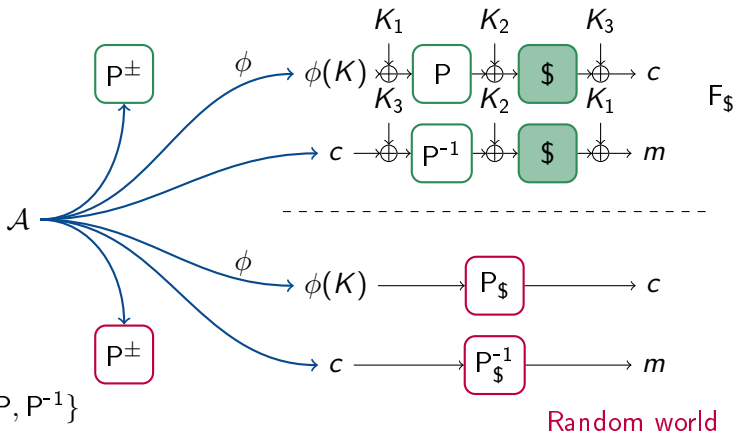


Game 1: Replace last  $P, P^{-1}$  with independent random permutations

# KDM security analysis: Splitting and forgetting technique

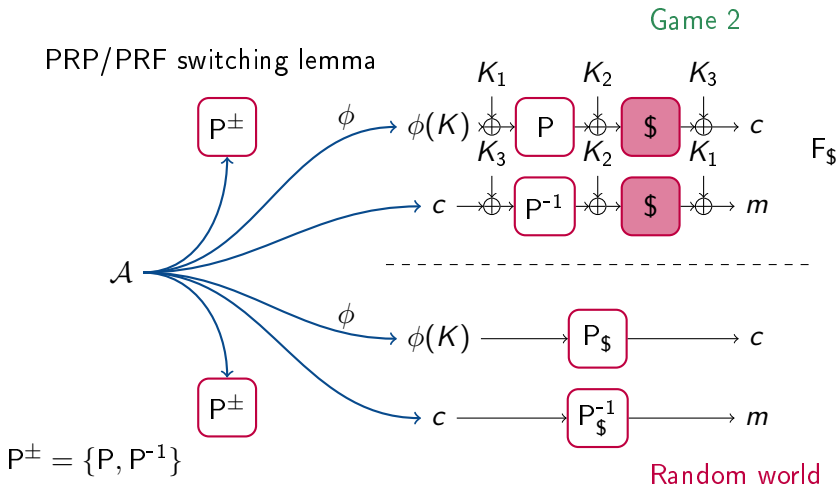
“Oracle forget”

Game 2



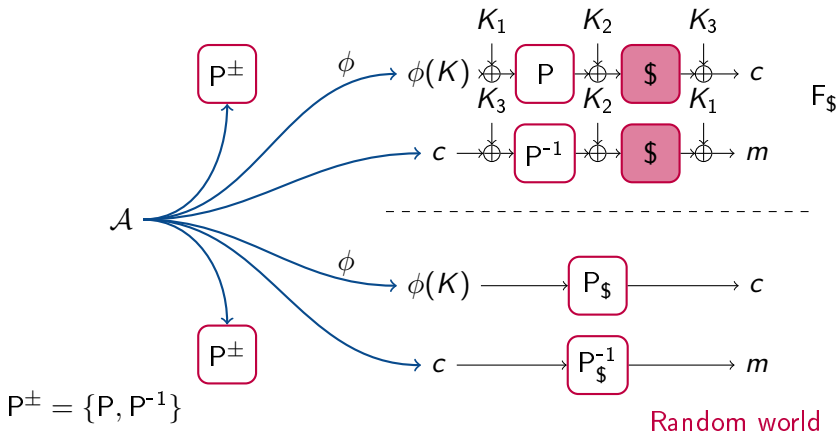
Game 2: Replace last  $P'$ ,  $P''$  with forgetful random oracles  $\$$

# KDM security analysis: Splitting and forgetting technique



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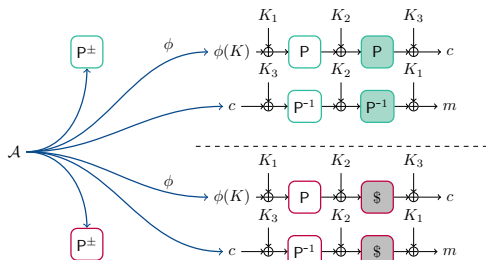
Game 2  $\approx$  Random world



Analysis of real world  $\approx$  random world?

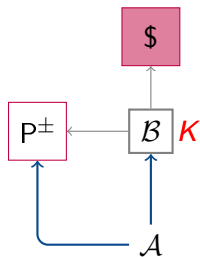
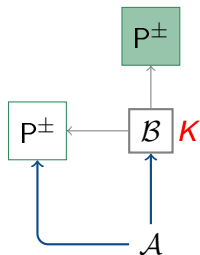
# Splitting and forgetting technique

Real world

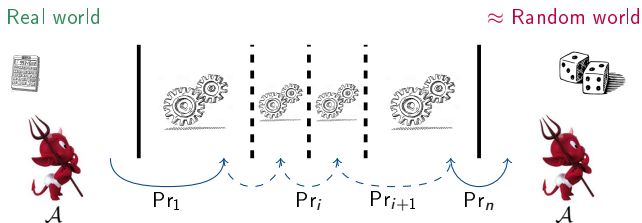


$\approx$  Random world

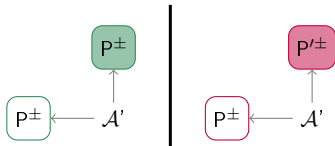
Simulator  $\mathcal{B}$  for challenge queries



# KDM security analysis: Splitting and forgetting technique

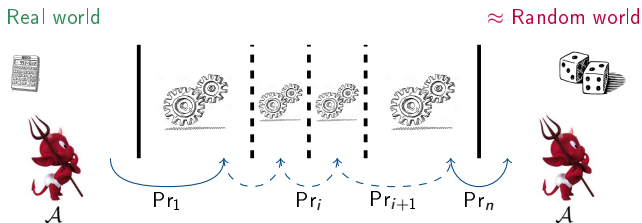


- Bad events between real world and  $\approx$  random world:
  - ▶ Reduction to adv “splitting game”



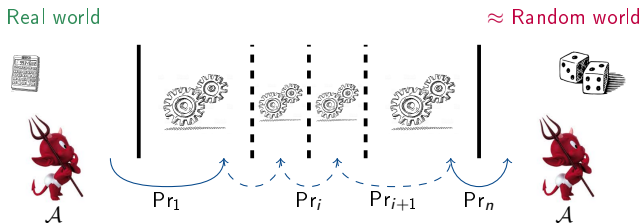


# KDM security analysis: Splitting and forgetting technique



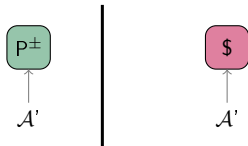
- Bad events between real world and  $\approx$  random world:
  - ▶ Reduction to adv “splitting game”
  - ▶  $Pr[sp]$  (splitting events type 1 and 2)

# KDM security analysis: Splitting and forgetting technique

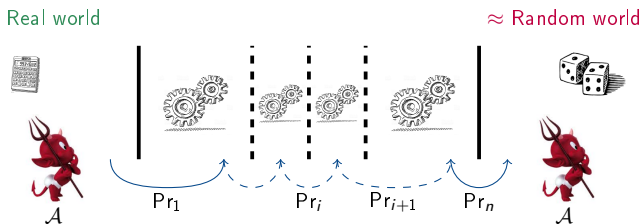


- Bad events between real world and  $\approx$  random world:

- ▶ Reduction to adv “splitting game”
- ▶  $Pr[sp]$  (splitting events type 1 and 2)
- ▶ Reduction to adv “forgetful switching game”



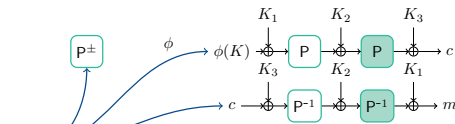
# KDM security analysis: Splitting and forgetting technique



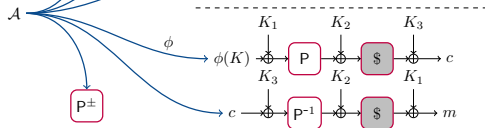
- Bad events between real world and  $\approx$  random world:
  - ▶ Reduction to adv “splitting game”
  - ▶  $Pr[sp]$  (splitting events type 1 and 2)
  - ▶ Reduction to adv “forgetful switching game”
  - ▶  $Pr[fg]$  (forgetful events)

# Splitting and forgetting technique

Real world



≈ Random world



$$\text{Adv}(\mathcal{A}) \leq 18q^2/2^n + q^2(2 \cdot \mathbf{Adv}^{cf}(\mathcal{A}_1) + \mathbf{Adv}^{ox}(\mathcal{A}_2))$$

when  $q_p = q$

offset-xor function:  $\phi(K) = K_i \oplus K_j \oplus \Delta$

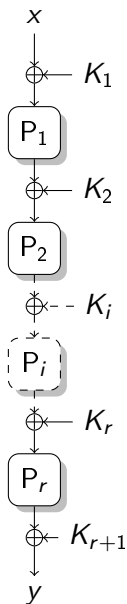
## Results: Even-Mansour

Rounds	Permutations	Key schedule	KDM set
1	$P$	$K_i =$	$cf \wedge offset$
2	$P_i \neq$	$K_i =$	$cf$
2	$P_i =$	$K_i \neq$	$cf \wedge ox$
2	$P_i =$	$K_i =$	$cf \wedge offset?$
3	$P_i =$	$K_i =$	$cf \wedge offset?$
3	$P_i =$	$K_i \neq$	$cf$

Security proofs [Farshim, K., Vergnaud]

On going work

Previous example



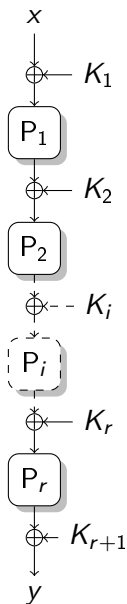
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2	$P_i =$	$K_i =$	cf $\wedge$ offset?
3	$P_i =$	$K_i =$	cf $\wedge$ offset?
3	$P_i =$	$K_i \neq$	cf

Security proofs [Farshim, K., Vergnaud]

On going work

IC KDM security level



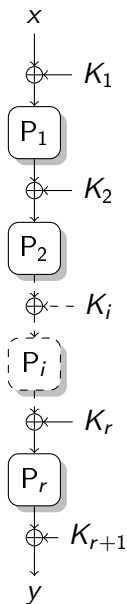
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2	$P_i =$	$K_i =$	$cf \wedge offset?$
3	$P_i =$	$K_i =$	$cf \wedge offset?$
3	$P_i =$	$K_i \neq$	$cf$

Security proofs [Farshim, K., Vergnaud]

On going work

Sliding attacks:  $P =$  and  $K =$



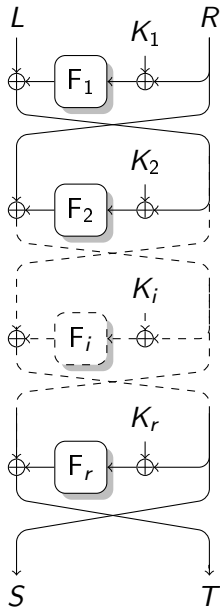
## Results: Key-Alternating Feistel

Rounds	Functions	Keys schedule	KDM set
4	$F =$	$K_1, 0, 0, K_2$	cf $\wedge$ offset $\wedge$ ox
4	$F_i \neq$	$K_i \neq$	cf $\wedge$ offset?
5	$F_i =$	$K_i \neq$	cf $\wedge$ offset?
?	$F_i =$	$K_i \neq$	cf

Security proof based on H-coefficient technique  
[Farshim, K., Seurin and Vergnaud]

Conjectures.

Open question: How many rounds with the same function needed to have KDM-security for a cf-set?





## Part 3.

# Incremental MACs

# Classical MAC algorithm

Document  $D$

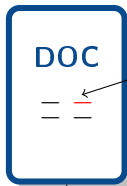


MAC(.)



$t$

Document  $D'$



MAC(.)



$t'$

Modification



Update expensive!  
Doc length dependent

# Incremental Cryptography: MAC

- Generate a tag  $t$  of a document  $D$ ,
- For each edition, the tag  $t$  is *updated*
  - ▶ Update in time dependent of modification size
  - ▶ Update time  $<$  MAC time



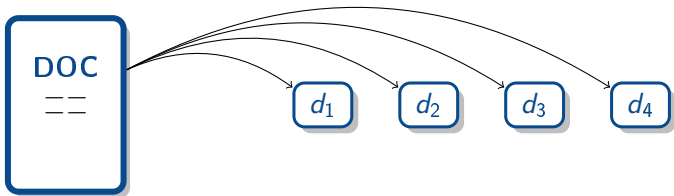
## Incremental MACs: the idea

Document  $D$



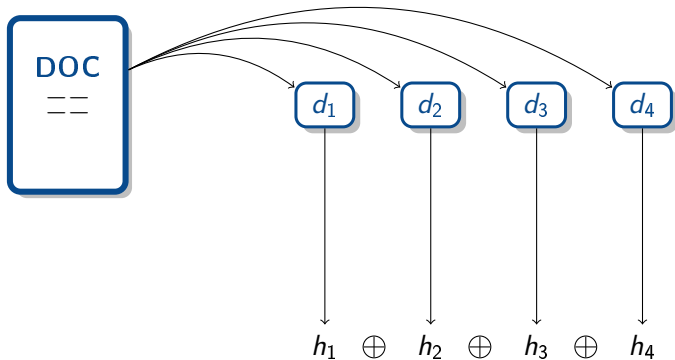
## Incremental MACs: the idea

Document  $D$



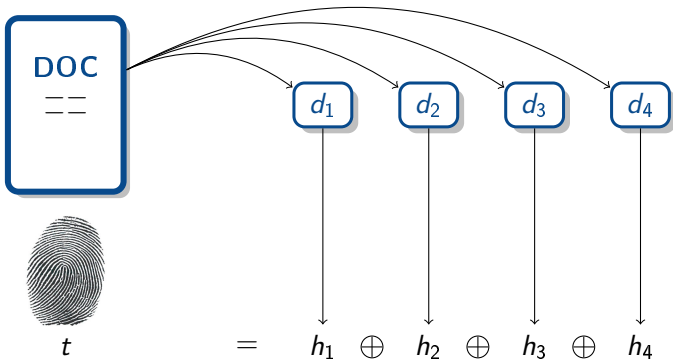
## Incremental MACs: the idea

Document  $D$



## Incremental MACs: the idea

Document  $D$



# Incremental Cryptography: MAC

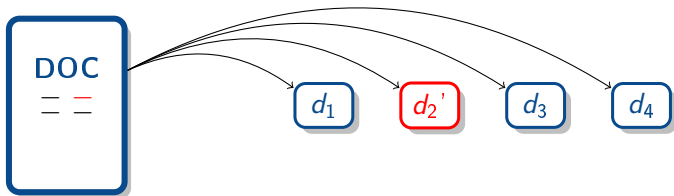
Document  $D'$





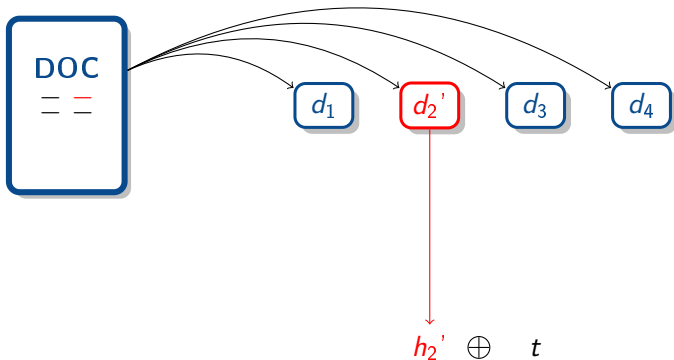
## Incremental Cryptography: MAC

Document  $D'$



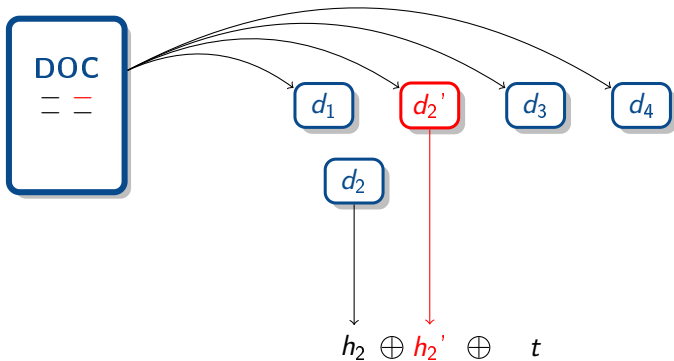
## Incremental Cryptography: MAC

Document  $D'$



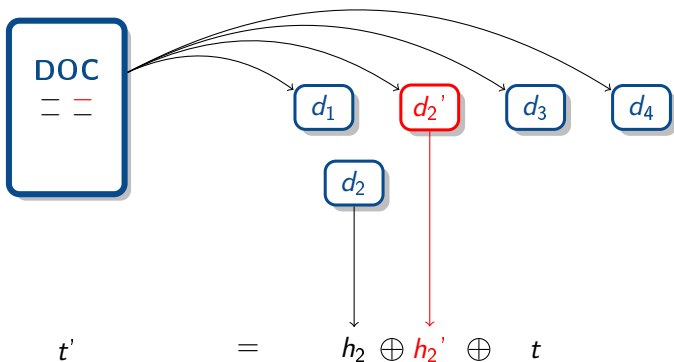
# Incremental Cryptography: MAC

Document  $D'$



## Incremental Cryptography: MAC

Document  $D'$



Tag independent from block order!

## Incremental MAC

An algorithm is incremental regarding specific *update* operations.

- Insert
- Delete
- Replace (possible using the previous operations)

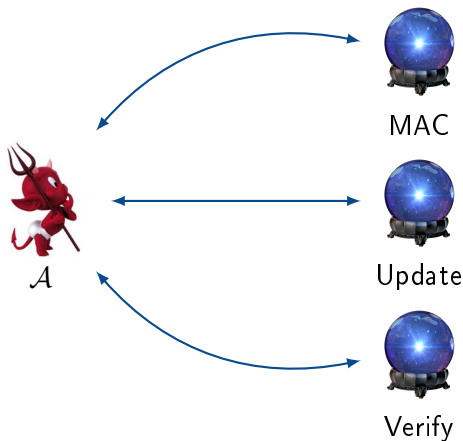
An update operation must be cheaper than recomputing a tag from scratch.

[BGG] Incremental Cryptography and Application to virus protection, Bellare, Goldreich, Goldwasser (1995):

- Security notions: **basic security** and **tamper-proof security**
- **Chained Xor-Scheme** (basic secure)

## Security Notion 1: Basic Security Model [BGG]

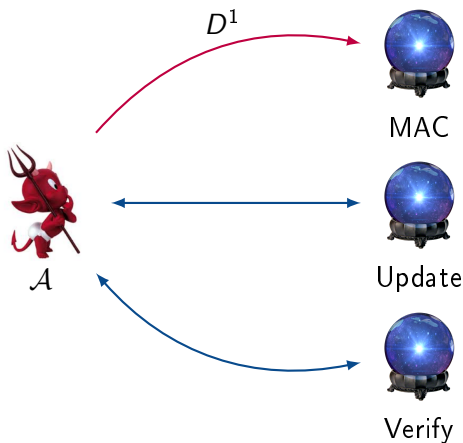
$\mathcal{L} := \{\}$



Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

# Security Notion 1: Basic Security Model [BGG]

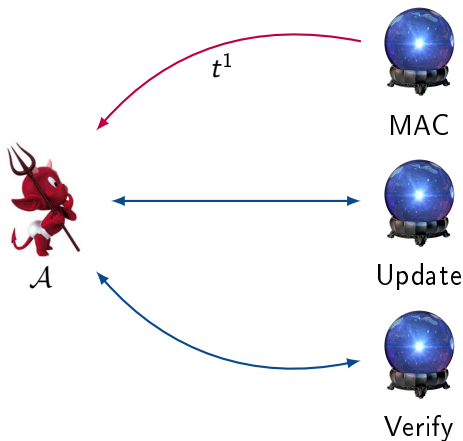
$\mathcal{L} := \{\}$



Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

# Security Notion 1: Basic Security Model [BGG]

$$\mathcal{L} := \{D^1\}$$

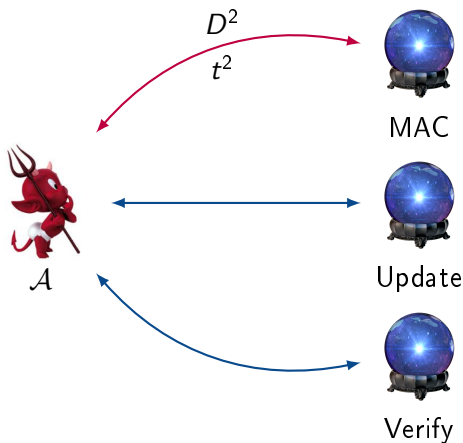


Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)



## Security Notion 1: Basic Security Model [BGG]

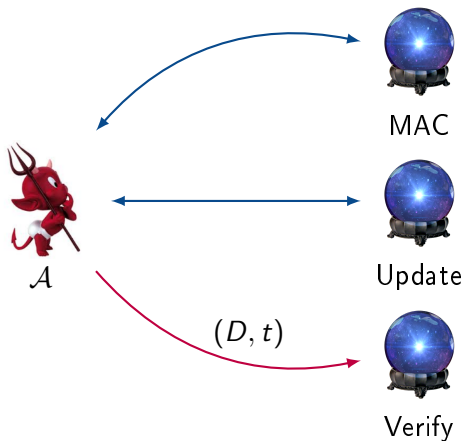
$$\mathcal{L} := \{D^1, D^2\}$$



Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

## Security Notion 1: Basic Security Model [BGG]

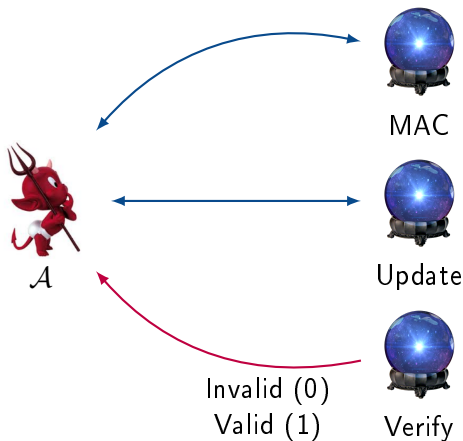
$$\mathcal{L} := \{D^1, D^2\}$$



Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

# Security Notion 1: Basic Security Model [BGG]

$$\mathcal{L} := \{D^1, D^2\}$$



Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

# Security Notion 1: Basic Security Model [BGG]

$\mathcal{L} := \{D^1, D^2\}$

op = Delete first block



$\mathcal{A}$

op,  $(D^2, t^2)$

Valid couple  $(D, t)$ !



MAC



Update



Verify

Only valid couples are updatable

Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

# Security Notion 1: Basic Security Model [BGG]

$$\mathcal{L} := \{D^1, D^2, D^3\}$$

op = Delete first block  
 $D^3 = \text{op}(D^2)$



A

op,  $(D^2, t^2)$

Valid couple  $(D, t)$ !

$t^3$



MAC



Update



Verify

Only valid couples are updatable

Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

# Security Notion 1: Basic Security Model [BGG]

$$\mathcal{L} := \{D^1, D^2, D^3, \dots, D^q\}$$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

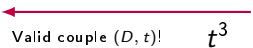
- $\text{Verify}(D^*, t^*)$  returns 1,
- $D^* \notin \mathcal{L}$ .



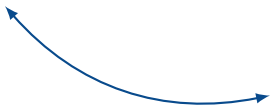
$\mathcal{A}$



MAC



Update



Verify

Only valid couples are updatable

Notations:  $D^i$  ( $i$ -th document) and  $D_j$  ( $j$ -th document block)

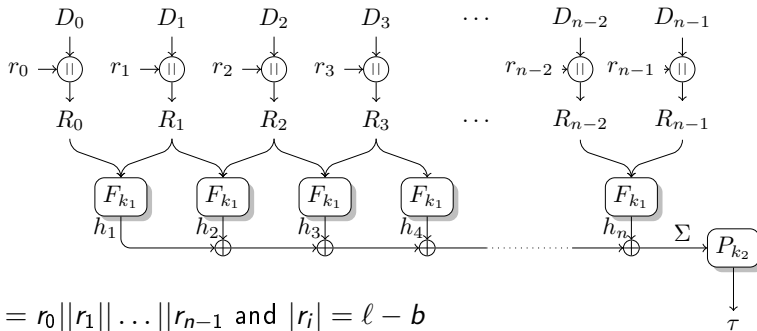
# Chained Xor-Scheme [BGG]

- Pair block chaining algorithm

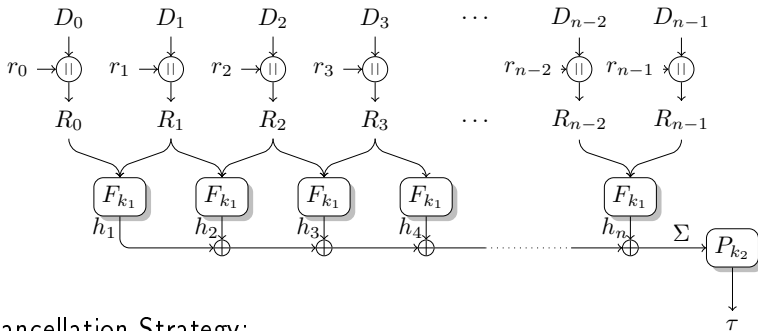
- $F : \mathcal{K}_F \times \{0,1\}^{2\ell} \rightarrow \{0,1\}^L$
- $P : \mathcal{K}_P \times \{0,1\}^L \rightarrow \{0,1\}^L$

- In: Document  $D$  ( $n$  blocks  $D_i$ )

- Out: Tag  $t$  such that  $t = (r, \tau)$



## Simple forgery strategy



Cancellation Strategy:

- $\mathcal{A}$  asks a MAC on any document  $D$  and receives  $t = (r, \tau)$
- Goal: Play with  $D$  to build  $D^*$  such that  $\Sigma = \Sigma^*$

[K. and Vergnaud]



## Example: 3-block document $D$

$$D = D_0 || D_1 || D_2$$

$$t = (r, \tau) \text{ such that } r := r_0 || r_1 || r_2$$

$$(R_i = D_i || r_i)$$

$$(R_0, R_1)$$

$$\downarrow$$

$$h_1$$

$$\oplus$$

$$(R_1, R_2)$$

$$\downarrow$$

$$h_2$$

$$= \Sigma$$

## Example: 3-block document $D$

$$D = D_0 || D_1 || D_2$$

$$t = (r, \tau) \text{ such that } r := r_0 || r_1 || r_2 \quad (R_i = D_i || r_i)$$

$$\begin{array}{ccc} (R_0, R_1) & & (R_1, R_2) \\ \downarrow & & \downarrow \\ h_1 & \oplus & h_2 \end{array} = \Sigma$$

Build  $D^*$  and  $r^*$  such that :

$$\begin{array}{ccccccc} (R_0, R_1) & & (.,.) & & (.,.) & & (R_1, R_2) \\ \downarrow & & \downarrow & & \downarrow & & \downarrow \\ h_1 & \oplus & \dots & \oplus & \dots & \oplus & h_2 \end{array} = \Sigma$$

$\underbrace{\quad \quad \quad}_{= 0}$

## Attack Example: 3-block document $D$

$$D = D_0 || D_1 || D_2 \text{ and } R_i = D_i || r_i$$

$$t = (r, \tau) \text{ such that } r := r_0 || r_1 || r_2$$

Build  $D^*$  and  $r^*$  such that:

$$\begin{array}{cccccc}
 (R_0, R_1) & (R_1, R_2) & (R_2, R_1) & (R_1, R_2) & (R_2, R_1) & (R_1, R_2) \\
 \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\
 h_1 & \cancel{h_2} & \cancel{h_2'} & \cancel{h_2} & \cancel{h_2'} & h_2
 \end{array} = \Sigma^*$$

$$\underbrace{\hspace{15em}}_{= 0}$$

$$D^* = D_0 || D_1 || D_2 || D_1 || D_2 || D_1 || D_2 \quad \tau^* = \tau \text{ and } t^* = (r^*, \tau^*)$$

$$r^* = r_0 || r_1 || r_2 || r_1 || r_2 || r_1 || r_2 \quad (D^*, t^*) \neq (D, t)$$

## Attack Example: 3-block document $D$

$$D = D_0 || D_1 || D_2 \text{ and } R_i = D_i || r_i \\ t = (r, \tau) \text{ such that } r := r_0 || r_1 || r_2$$

Build  $D^*$  and  $r^*$  such that:

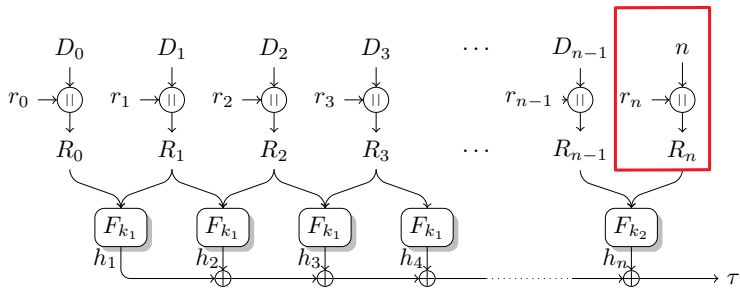
$$\begin{array}{cccccc} (R_0, R_1) & (R_1, R_2) & (R_2, R_1) & (R_1, R_2) & (R_2, R_1) & (R_1, R_2) \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ h_1 & \cancel{h_2} & \cancel{h_2'} & \cancel{h_2} & \cancel{h_2'} & h_2 \end{array} = \Sigma^*$$

$\underbrace{\hspace{15em}}_{= 0}$

$$D^* = D_0 || D_1 || D_2 || D_1 || D_2 || D_1 || D_2 \quad \tau^* = \tau \text{ and } t^* = (r^*, \tau^*) \\ r^* = r_0 || r_1 || r_2 || r_1 || r_2 || r_1 || r_2 \quad (D^*, t^*) \neq (D, t)$$

More attacks in the thesis.

## Modified Xor-Scheme 2



- A **fresh** value  $r_n$  for each update operation
- The random value  $r_n$  is necessary!

Basic secure scheme

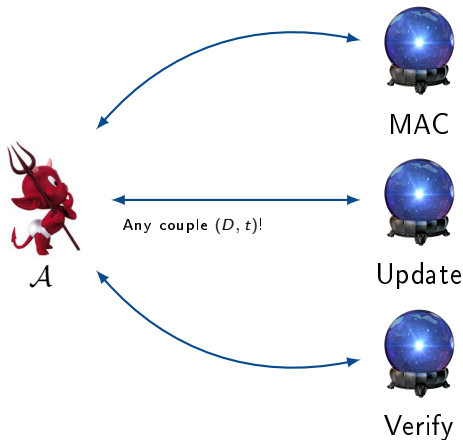
## Security Notion 2: Tamper-proof Security Model [BGG]

$\mathcal{L} := \{\}$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$



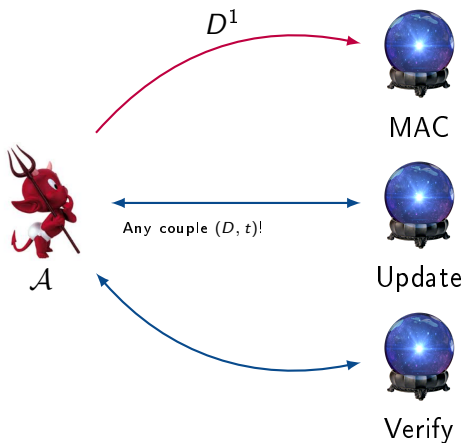
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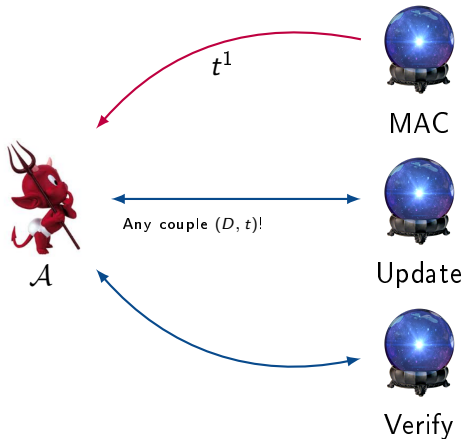
## Security Notion 2: Tamper-proof Security Model [BGG]

$$\mathcal{L} := \{D^1\}$$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$





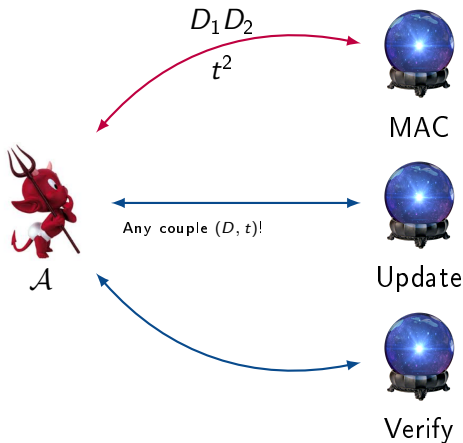
## Security Notion 2: Tamper-proof Security Model [BGG]

$$\mathcal{L} := \{D^1, D_1D_2\}$$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$



## Security Notion 2: Tamper-proof Security Model [BGG]

$$\mathcal{L} := \{D^1, D_1D_2\}$$

op = Replace block 1 by  $D_1'$   
 $D^3 = \text{op}(?)$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$



$\mathcal{A}$

op,  $(D_1D_2', t^2)$

Any couple  $(D, t)$ !



MAC



Update



Verify

## Security Notion 2: Tamper-proof Security Model [BGG]

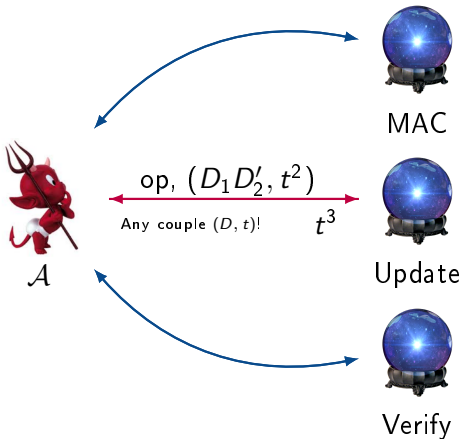
$$\mathcal{L} := \{D^1, D_1D_2, D'_1D'_2?\}$$

op = Replace block 1 by  $D_1'$   
 $D^3 = \text{op}(?)$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$



## Security Notion 2: Tamper-proof Security Model [BGG]

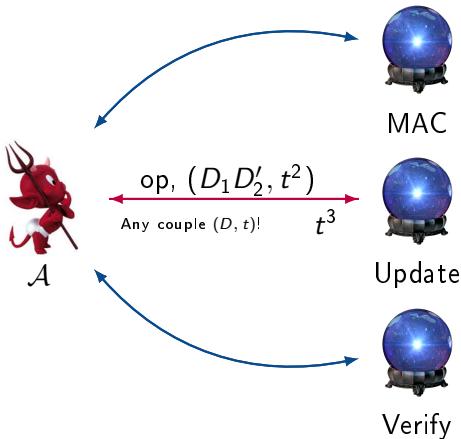
$$\mathcal{L} := \{D^1, D_1D_2, D'_1D'_2?, \\ \text{or } D'_1D_2? \text{ or both?}\}$$

op = Replace block 1 by  $D_1'$   
 $D^3 = \text{op}(?)$

Winning conditions:

$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$



## Security Notion 2: Tamper-proof Security Model [BGG]

$$\mathcal{L} := \{D^1, D_1D_2, D'_1D'_2?, \\ \text{or } D'_1D_2? \text{ or both?}\}$$

op = Replace block 1 by  $D_1'$   
 $D^3 = \text{op}(?)$

Winning conditions:

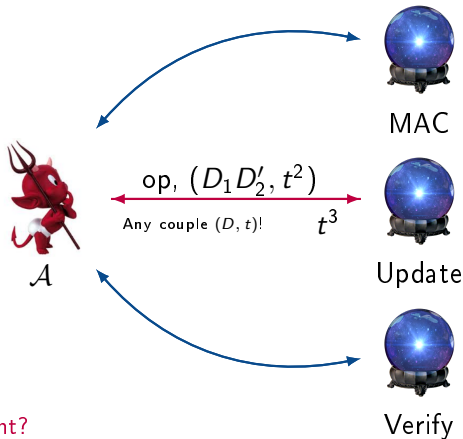
$\mathcal{A} \rightarrow (D^*, t^*)$  such that:

- $\text{Verify}(D^*, t^*)$  returns 1
- $D^* \notin \mathcal{L}$

But how to build  $\mathcal{L}$ ?

How can we track each document?

No game definition...

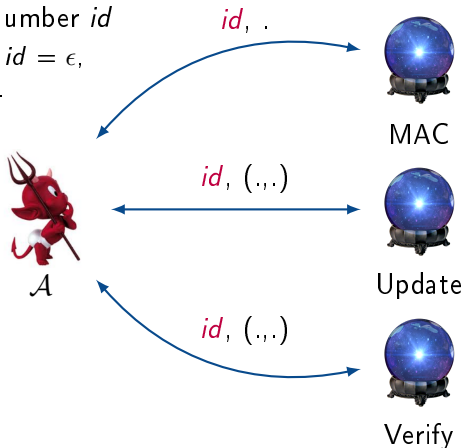


$\implies$  Introduction of the document identification number  $id$

## New Framework for iMAC

- Document identification number  $id$ 
  - ▶ Single-document (SD)  $id = \epsilon$ ,
  - ▶ Multi-document (MD).

One MAC call/ $id$



# New Framework for iMAC

- Document identification number  $id$

- ▶ Single-document (SD)  $id = \epsilon$ ,
- ▶ Multi-document (MD).

One MAC call/ $id$



$id, .$



MAC

$id, (.,.)$



Update

$id, (.,.)$



Verify

- Incremental UnForgeability (IUF)

- ▶ Type 1 (IUF1)  $\approx$  Basic Security
- ▶ Type 2 (IUF2)  $\approx$  Tamper-proof Security

# Security game IUF1

- Definition close to Basic security

- List  $\mathcal{L}$

- 1  $D^1$   $D^2$
- 2  $D^1$   $D^2$
- 3  $D^1$

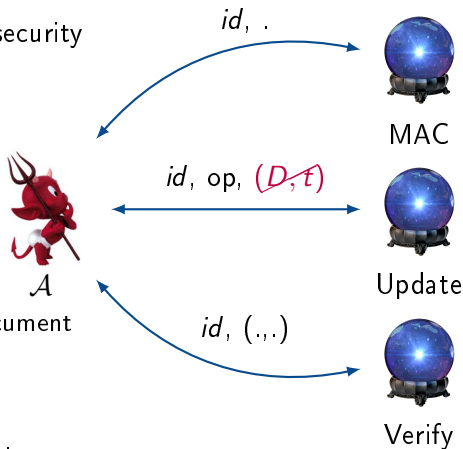
- For each  $id$

- ▶ Last version of the document updated

- Winning conditions:

$\mathcal{A} \rightarrow (id, D^*, t^*)$  such that:

- ▶  $\text{Verify}(id, D^*, t^*)$  returns 1,
- ▶  $(id, D^*) \notin \mathcal{L}$ .





## Security game IUF2

- Definition close to Tamper-proof security

- List  $\mathcal{L}$

- 1  $D^1 \rightarrow D^2$
- 2  $D^1 \rightarrow D^2$
- 3  $D^1$

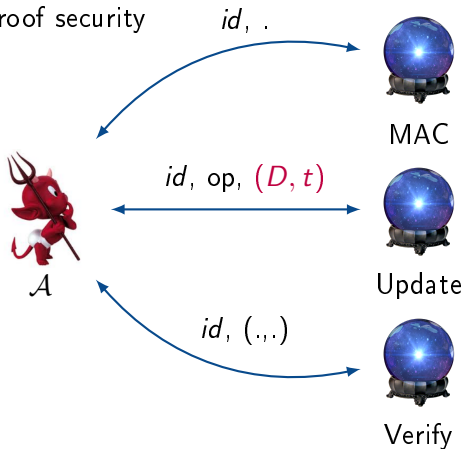
- For each  $id$

- ▶ tag: Computed with  $D$
- ▶ List: Filled with  $op(D_{id})$

- Winning conditions:

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## Security game IUFR ("Replay")

- IUF1R or IUF2R

- List  $\mathcal{L}$  (last doc/  $id$ )

- 1  $D^7$
- 2  $D^4$
- 3  $D^1$

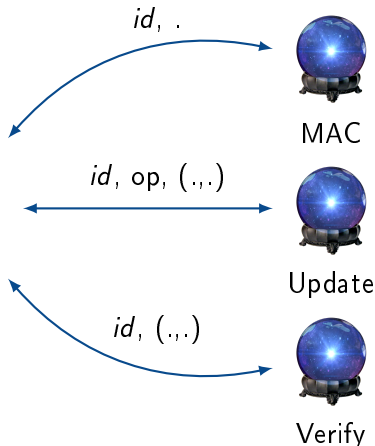
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$\mathcal{A}$



FADE mechanism

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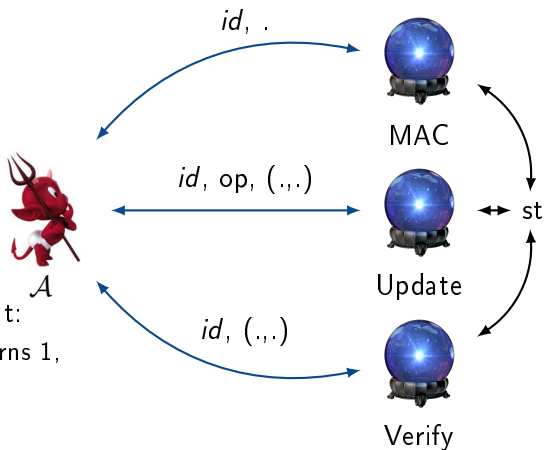
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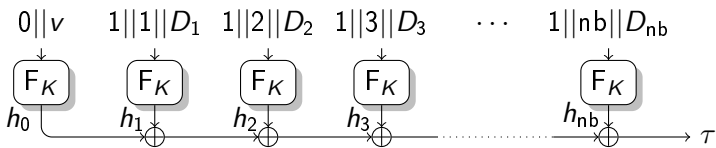
- Stateful Schemes only

- ▶ (Secure memory)



FADE mechanism

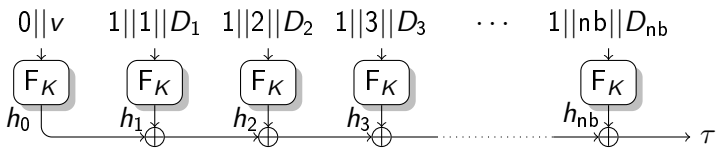
## Results: Constructions



From a basic secure Xor-MAC to a IUF1R-MD construction.

- Xor-MAC is basic secure
  - ▶ "Xor-MACs: New Methods for Message Authentication Using Finite Pseudorandom Functions", Bellare, Guérin, Rogaway.
- Basic security  $\implies$  IUF1-SD
- A construction IUF1R-MD
  - ▶ Generic construct.: SD to MD
  - ▶ Generic construct.: IUF<sub>x</sub> to IUF<sub>x</sub>R

## Results: Constructions

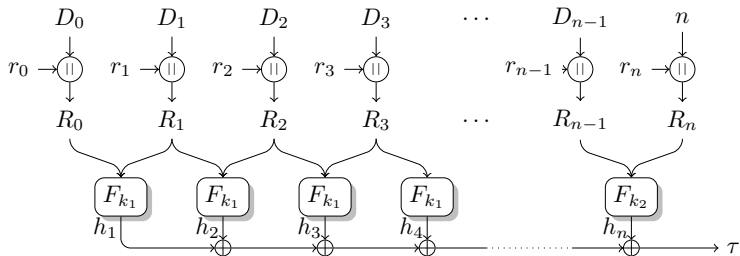


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Not IUF2

## Results: Constructions

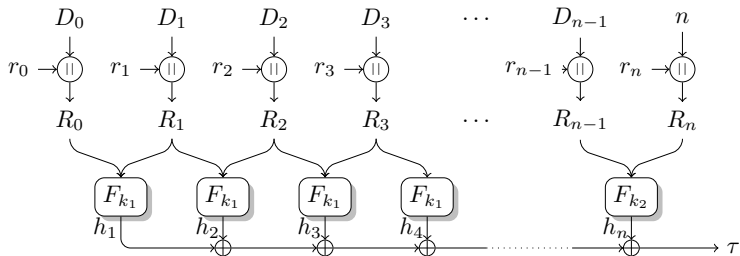


From an IUF2-SD secure XOR-Scheme to IUF2R-MD secure construction.

- Xor-Scheme proved IUF2-SD
- A IUF2R-MD secure construction
  - ▶ Generic construct.: SD to MD,
  - ▶ Generic construct.: IUFx to IUFxR.

[Arte, Bellare, K. and Vergnaud].

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Strongest security notion

[Arte, Bellare, K. and Vergnaud].

# Conclusion

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  - ▶ Forgetting and splitting (application EM)
  - ▶ H-coefficient technique (application KAF)



# Conclusion

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    - Tag too large,
    - Greedy in randomness.

## Conclusion

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    - Tag too large,
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  - ▶ More efficient schemes (time/storage)?
    - Can we build such a scheme ?
  - ▶ What about implementation?

Thank you for your attention!

# Full Disk Encryption and Beyond

Monday, 15 July 2019

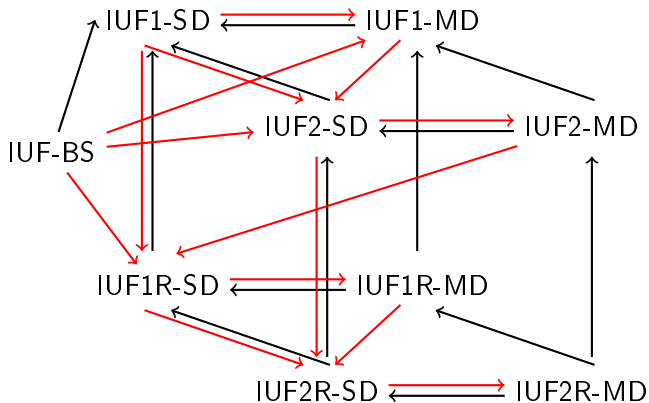


Louiza Khati

## Contributions

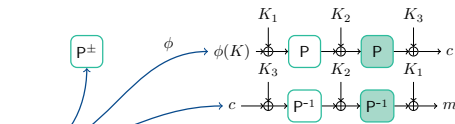
- FDE: Bridging theory and practice, RSA 2017
  - ▶ K., Mouha and Vergnaud.
- Even-Mansour cipher under KDM security, FSE 2018
  - ▶ Farshim, K. and Vergnaud
- KDM-Security of Key-Alternating Feistel Ciphers
  - ▶ Farshim, K., Seurin and Vergnaud
- Analysis and improvement of an incremental scheme, SAC 2018
  - ▶ K. and Vergnaud
- Incremental MACs
  - ▶ Arte, Bellare, K. and Vergnaud.

## Relations among security notions

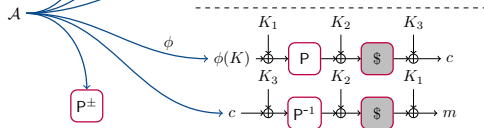


# Splitting and forgetting technique

Real world



≈ Random world



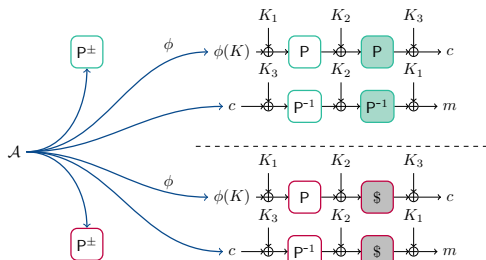
$$\text{Adv}(\mathcal{A}) \leq 18q^2/2^n + q^2(2 \cdot \mathbf{Adv}^{cf}(\mathcal{A}_1) + \mathbf{Adv}^{ox}(\mathcal{A}_2))$$

when  $q_p = q$

offset-xor function:  $\phi(K) = K_i \oplus K_j \oplus \Delta$

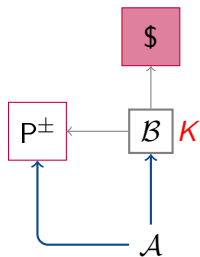
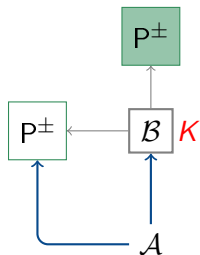
# Splitting and forgetting technique

Real world



$\approx$  Random world

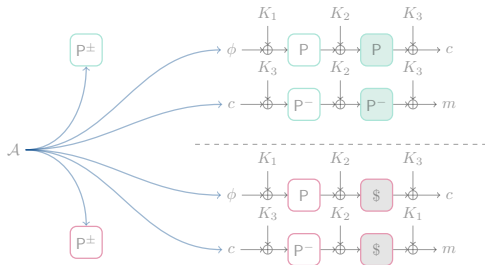
2-round Even-Mansour



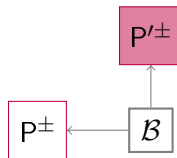
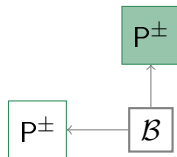


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Real world



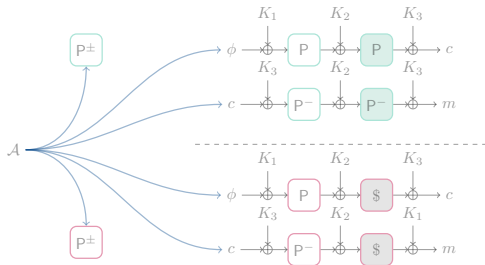
$\approx$  Random world



Splitting game

# Splitting and forgetting technique

Real world



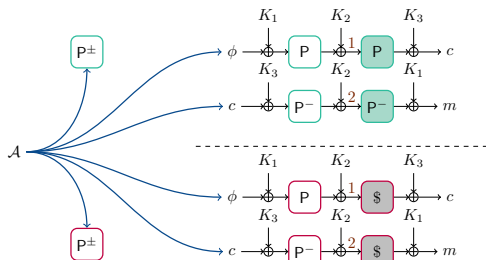
$\approx$  Random world



Forgetful switching game

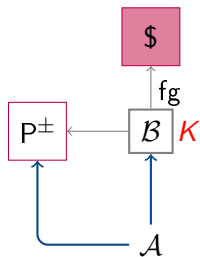
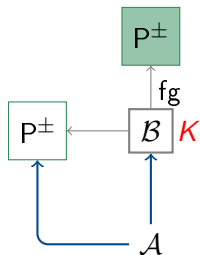
# Splitting and forgetting technique

Real world



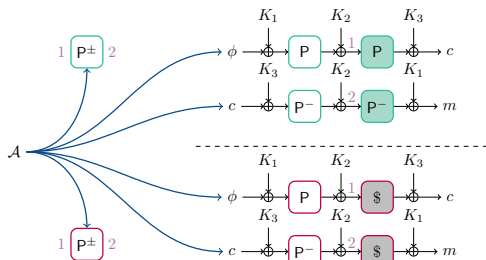
$\approx$  Random world

Forgetful events



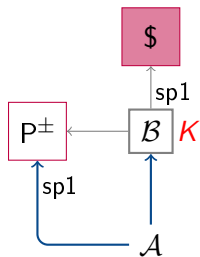
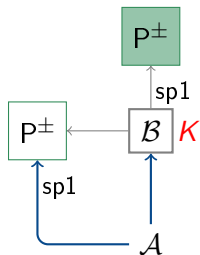
# Splitting and forgetting technique

Real world



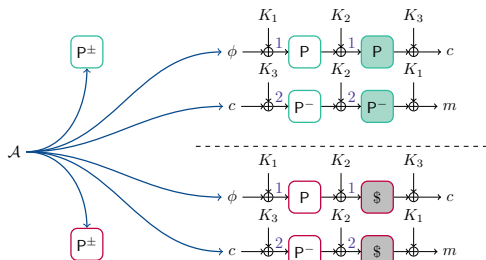
$\approx$  Random world

Splitting events 1



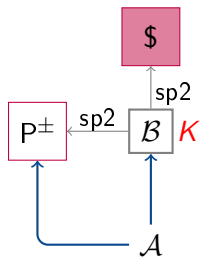
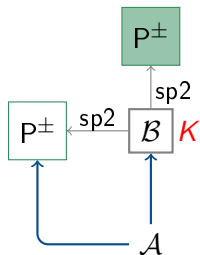
# Splitting and forgetting technique

Real world



≈ Random world

Splitting events 2



# Splitting and forgetting technique

